Optimization of Bistability in Nonlinear Chalcogenide Fiber Bragg Grating for All Optical Switch and Memory Applications

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ABSTRACT—We solve the coupled mode equations governing the chalcogenide nonlinear fiber Bragg gratings (FBGs) numerically, and obtain the bistability characteristics. The characteristics of the chalcogenide nonlinear FBGs such as: switching threshold intensity, bistability interval and on-off switching ratio are studied. The effects of FBG length and its third order nonlinear refractive index on FBG characteristics are investigated. We obtain an interesting result that independent of the third order nonlinear refractive index; there exists an optimum FBG length of about 6 mm at which the on-off switching ratio becomes maximized. It is also found that by increasing the nonlinearity, the maximum value of on-off switching ratio decreases. The results of this paper can be mainly used for designing all-optical switches and memories.

KEYWORDS: Nonlinear fiber Bragg grating (FBG), optical bistability, bistability characteristics, all optical memory, all optical switch.

I. INTRODUCTION

Because of growing fiber Bragg grating (FBG) applications in optical communication systems [1-3] and optical fiber sensors [4], they will play a crucial role in future all-optical communication [5]. A considerable advantage of nonlinear FBGs is that they can be designed as all optical switches [6-8] and optical bistable devices [9-11]. The study of optical switching and optical bistability has been started since 1979 [12]. Using common silica FBGs, these phenomena require high peak intensity in the order of GW/cm^2 [3]. Until recently, when using chalcogenide FBGs, the required peak intensity for optical bistability has been decreased 1000 times, because of their higher third order nonlinear coefficient compared to the silica one [13, 14]. Therefore, shorter length is needed to create high quality bistability and switching phenomena when chalcogenide FBG is used.

In the present paper, the optical bistability in chalcogenide fiber Bragg gratings with third order nonlinearity is studied numerically. The effects of fiber length and third order nonlinear refractive index on switching threshold intensity, bistability interval and ratio of on-off switching will be studied in section 3. Finally, optimization of switching and bistability with regards to input intensity, FBG length and nonlinear coefficient of chalcogenide materials is carried out. The obtained results are helpful for future design of all-optical memories and switches.

II. THEORY AND NUMERICAL CALCULATIONS

Consider a lossless uniform FBG with length of L which is shown in Fig. 1.

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The refractive index of a uniform fiber Bragg grating as a function of position, *z* and electric field in the FBG, *E* can be written as [15]:

$$n(z) = n_0 + n_1 \cos\left(\frac{2\pi}{\Lambda} z\right) + n_2 |E|^2, \quad (1)$$

where Λ is the FBG period, n_0, n_1 and n_2 are the linear refractive index, refractive index modulation amplitude, and third order nonlinear refractive index coefficient, respectively.

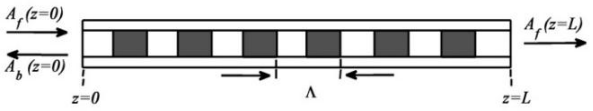


Fig. 1. The schematic diagram of the FBG with length of L. The forward and backward waves are shown.

By combining forward and backward waves, the electric field in the FBG can be described as [15]:

$$E(\mathbf{r},t) = \frac{1}{2} F(x,y)\Big[A_f(z,t) e^{i\beta_B z} + A_b(z,t) e^{-i\beta_B z} \Big] e^{-i\omega_0 t} + c.c., \quad (2)$$

where A_f and A_b are the slowly varying amplitude of forward and backward waves respectively and ω_0 is the carrier frequency. F(x,y) is the transverse variations of the two counter-propagating waves.

In this paper, we take continuous wave (CW) limit by neglecting the time derivatives as it is discussed in [16]. By substitution of Eqs. (1) and (2) into the Maxwell's wave equations and considering slowly varying amplitude approximation, the nonlinear coupled mode equations for both forward and backward wave amplitudes can be obtained as follows [15, 16]:

$$\frac{\partial A_f}{\partial z} + \frac{\alpha}{2} A_f = i\delta A_f + i\kappa A_b + i\gamma\left(|A_f|^2 + 2|A_b|^2\right) A_f, \quad (3)$$

$$-\frac{\partial A_b}{\partial z} + \frac{\alpha}{2} A_b = i\delta A_b + i\kappa A_f + i\gamma\left(|A_b|^2 + 2|A_f|^2\right) A_b, \quad (4)$$

where α represents the FBG loss which is neglected here, δ, κ and γ account for detuning from the Bragg wavelength, coupling coefficient, and nonlinear coefficient, respectively.

By applying 4th order Rung-Kutta numerical method, we solve the aforementioned coupled mode nonlinear equations numerically.

As it is discussed in [2, 5, 17], we perform these calculations from the end of the FBG to its beginning using boundary conditions of $A_f(z=L) = A_{fL}$, $A_b(z=L) = 0$, where A_{fL} is an adjustable value for better simulation. The results are shown in Figures 2-10.

III. RESULTS AND DISCUSSION

As shown in Fig. 2 a typical optical bistability diagram contains three branches: low, medium, and high branch which are shown by AB, BE and ED lines, respectively. The middle branch, i.e. BE, is unstable and reaching to it is almost impossible in practice. Bistability interval, on-off switching ratio, and switching threshold intensity are three important parameters of optical bistability, as presented in Fig. 2. The bistability interval is the interval of input intensities in which the bistability diagram has two stable outputs. The on-off switching ratio is the amount of change in the output intensity when switching on is occurring, and the switching threshold intensity is the minimum input intensity required for switching on i.e. for transition from low branch to the high branch in bistability curve. Typical values of parameters used in this paper are shown in Table 1. We study the effect of some of these parameters on bistability characteristics such as switching threshold intensity, bistability interval and ratio of on-off switching.

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Table 1. Typical data used in this work.

$\lambda_B = 1550\,\text{nm}$	$n_0 = 2.54$	$n_2 = 220\, n_{2silica}$	[18]
$\lambda = 1550.015\,\text{nm}$	$n_1 = 1.5\times10^{-4}$	$n_{2silica} = 0.273\times10^{-19}\, m^2/W$	[19]
	$\Lambda = 3.1631\times10^{-7}\, m$		

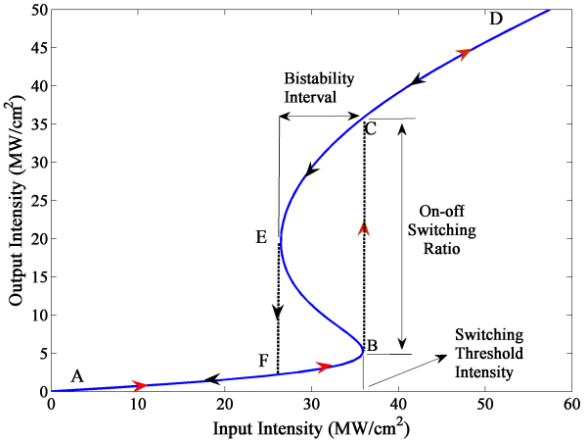


Fig. 2. Typical optical bistability diagram.

A. *Effect of fiber length on optical bistability*

Since FBG length is normally introduced by $L = N_L \Lambda$, where N_L is the number of FBG periods, we follow the same notation and use N_L instead of L. The effect of FBG period on bistability diagram was studied. The range of FBG period was 15000-23000 corresponding to FBG lengths of 4.7-7.9 mm.

The results are depicted in Fig. 3. The lowest value of the number of FBG periods (FBG's length) is chosen to be near to the onset of bistability. This figure shows that increasing the number of the FBG periods, improves the bistability and also there is a minimum length below which there is no bistability. There are two possible reasons for this behavior. First, by increasing the length, nonlinearity increases. Second, by increasing the length, the output intensity is amplified even greater than the input intensity of the FBG which intensifies the nonlinearity effect as can be seen in Fig.4. In this figure the intensity of transmitted light is presented as a function of position, for n_2=220 $n_{2silica}$. The intensity of input wave is 1 MW/cm^2. As the intensity of field increases in the fiber so does the nonlinear effect. Due to the nonlinear effect and reflecting from periodic structure of Bragg grating, the intensity of transmitted field increases in the fiber. It is an interesting phenomenon that the intensity of filed in the FBG can be greater than the input intensity. Due to these two main causes, the nonlinearity is increased, which leads to improvement of the bistability and as a result the switching threshold intensity is decreased. Fig. 3 shows the switching threshold intensity and the bistability interval with regard to the length of fiber. This figure indicates the improvement of bistability, i.e. decreasing the switching threshold by increasing the length.

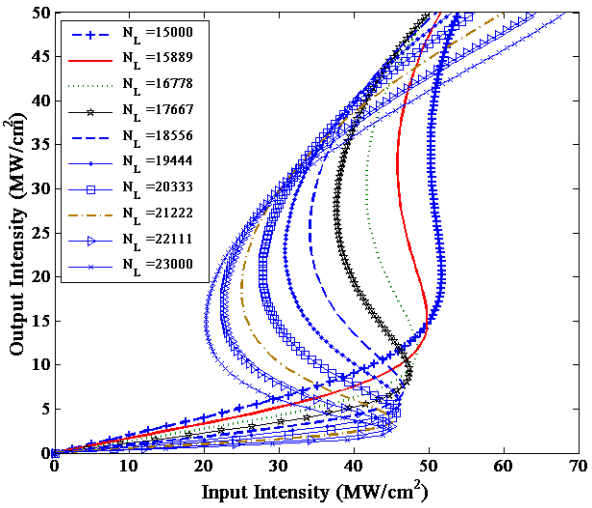


Fig. 3. The effect of number of FBG periods on optical bistability characteristics.

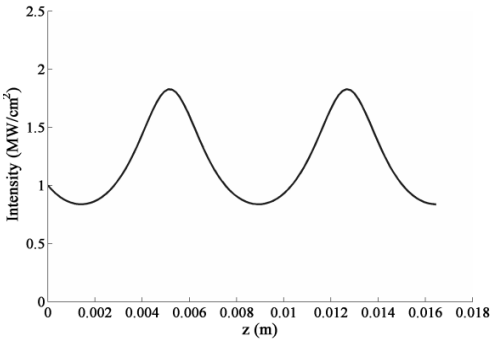


Fig. 4. The intensity of light transmitted in the FBG as a function of position.

The on-off switching ratio as a function of number of FBG periods is shown in Fig. 6. The result of this figure is considerable because it shows that the on-off switching ratio diagram has a maximum value at a specific number of FBG periods. In other

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words there is an optimum FBG length at which the switching reaches its maximum value and it is important for designing FBGs with better switching behavior. The maximum of on-off switching ratio is almost occurred at $N_L = 18800$ corresponding to L=5.9 mm.

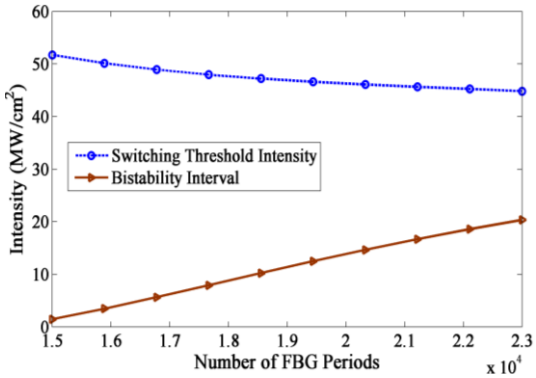


Fig. 5. The effect of number of FBG periods on bistability interval and switching threshold intensity.

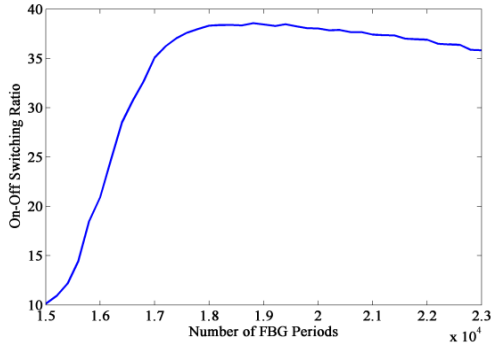


Fig. 6. The on-off switching ratio as a function of number of FBG periods.

B. *Effect of third order nonlinear refractive index on optical bistability*

Chalcogenide materials have a wide range of nonlinearity ranging from about 100 to 1000 times of the fused silica as indicated in Table 2. The bistability characteristics depend on third order nonlinear refractive index. Naturally by increasing the third order nonlinear refractive index the bistability improves and hence we studied its effect on bistability characteristic numerically. The results of our simulations are illustrated in Fig. 7. Each curve of this figure refers to a specific value of third order nonlinear refractive index which is selected from Table 2. The results evidently illustrate that increasing the nonlinearity improves the desired bistability parameters. The connection between the parameters and bistability are presented in Fig. 8. This figure indicates the reduction of switching threshold due to increment of the third order nonlinear refractive index, as expected and desired. In addition, it shows that the bistability interval and on-off switching ratio decrease when the third order nonlinear refractive index increases. Therefore depending on the FBG application i.e. optical switch or optical bistable device, suitable chalcogenide material can be selected.

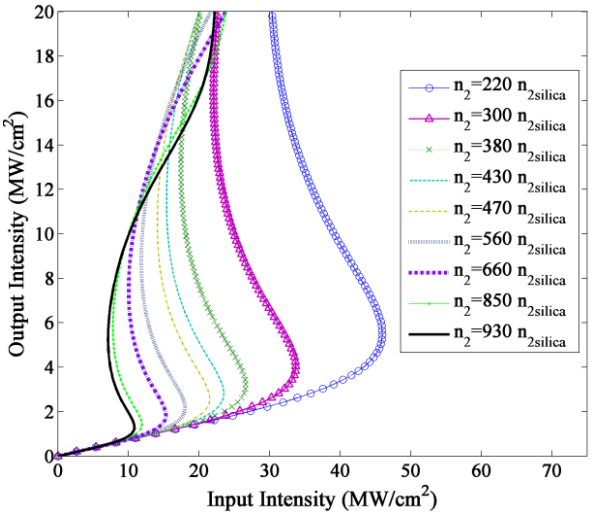


Fig. 7. Optical bistability curves for nine chalcogenide glasses of different third order nonlinear refractive indices.

Table 2. n_0 and n_2 parameters of chalcogenide glasses [18].

Glass	n_0 at 1.55 µm	$n_2/n_{2silica}$ (±15%)
$As_{40}S_{60}$	2.45	220
$As_{40}S_{40}Se_{20}$	2.55	300
$As_{40}S_{50}Se_{10}$	2.49	380
$As_{40}S_{30}Se_{30}$	2.62	430
$As_{25}S_{55}Te_{20}$	2.52	470
$As_{40}S_{10}Se_{50}$	2.76	560
$As_{30}Se_{61}$	2.81	660
$As_{40}Se_{55}Cu_5$	2.93	850
$As_{40}Se_{60}$	2.81	930

C. *Optimum fiber length for various third order nonlinear coefficients*

The on-off switching ratio versus the number of FBG periods for nine chalcogenide glasses of different third order nonlinear refractive indices is plotted in Fig. 9. It may be expected that by increasing the third order refractive index, we have a lower optimum length. However, the results show otherwise. We

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found that the optimum length for maximizing the on-off switching ratio is nearly independent of n_2. This optimum FBG length is about 6 mm as shown in Fig. 10.

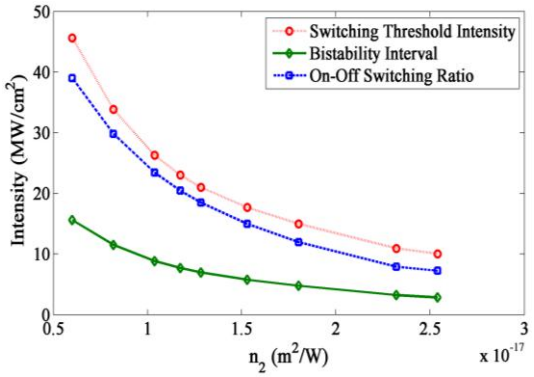


Fig. 8. The diagrams of switching threshold, bistability interval and on-off switching ratio versus third order nonlinear refractive index.

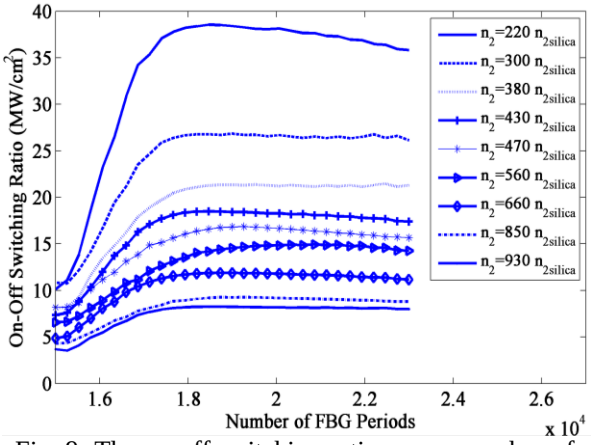


Fig. 9. The on-off switching ratio versus number of FBG periods for nine chalcogenide glassess of different third order refractive indicies .

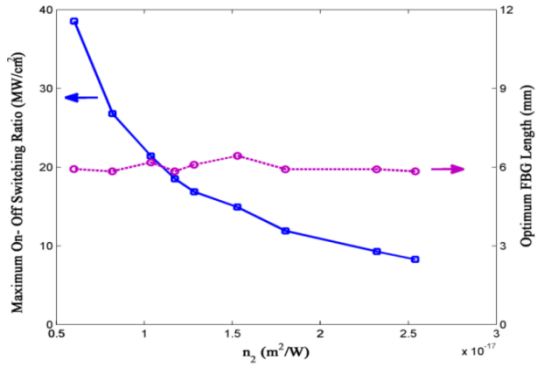


Fig. 10. The maximum on-off switching ratio and optimum FBG length versus third order refractive index of chalcogenide glassess.

Fig. 9 also indicates that increasing the third order refractive index makes the on-off switching ratio more stable and flatted above the optimum length. These results are useful and important for designing optical switches and memories.

As seen in Fig. 10, by increasing the third order nonlinear refractive index the maximum on-off switching ratio is decreased however the optimum FBG length is almost constant. In Table 3, the Suitable range of bistability parameters for optical switch and memory applications is qualitatively shown. As shown in this Table the high range of on-off switching ratio as well as low range of switching threshold, is suitable for both optical switch and memory devices. However the desired value of bistability interval depends on application. For switching application low range of bistability interval is required, while, the bistability interval of optical memories should be sufficiently high.

Tabel 3. Suitable range of bistability parameters for optical switch and memory applications.

Bistability characteristic	**Low**	**High**
On-off switching ratio	---	Optical switch and optical memory
Switching threshold	Optical switch and optical memory	---
Bistability interval	Optical switch	Optical memory

IV. CONCLUSION

By numerical calculations, we solved the nonlinear coupled mode equations which govern the pulse propagation through FBG and derived the bistability diagram. We investigated the effects of two important parameters: FBG length and third order nonlinear refractive index. Finally by comparing the bistability diagrams the following results are found: First, the switching threshold is decreased by increasing FBG length as well as third order refractive index. Second, the bistability interval can be increased by increasing the FBG length or by decreasing the third order refractive index. Third, the on-off switching ratio is decreased by increasing the third order nonlinear refractive index. Finally, independent of the third order refractive index, an optimum FBG length of about 6 mm at which the on-off switching ratio is maximized was found. These

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results are the base of planning and designing all-optical integrated devices such as flip-flops.

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